

Decision Making with Multiple Agents that Care about More than One Objective

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 @DiederikRo @rox_teo #aamasT1

AAMAS Tutorial 1, London, 2023

Pleased to meet you



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Hi, I'm Diederik!

- Academic Liaison for AI Research
Urban Innovation and R&D, City of Amsterdam
- Senior Researcher
AI lab, Vrije Universiteit
Brussel



 @DiederikRo

Sources: [here](#) and [here](#)

Hi, I'm Roxana!



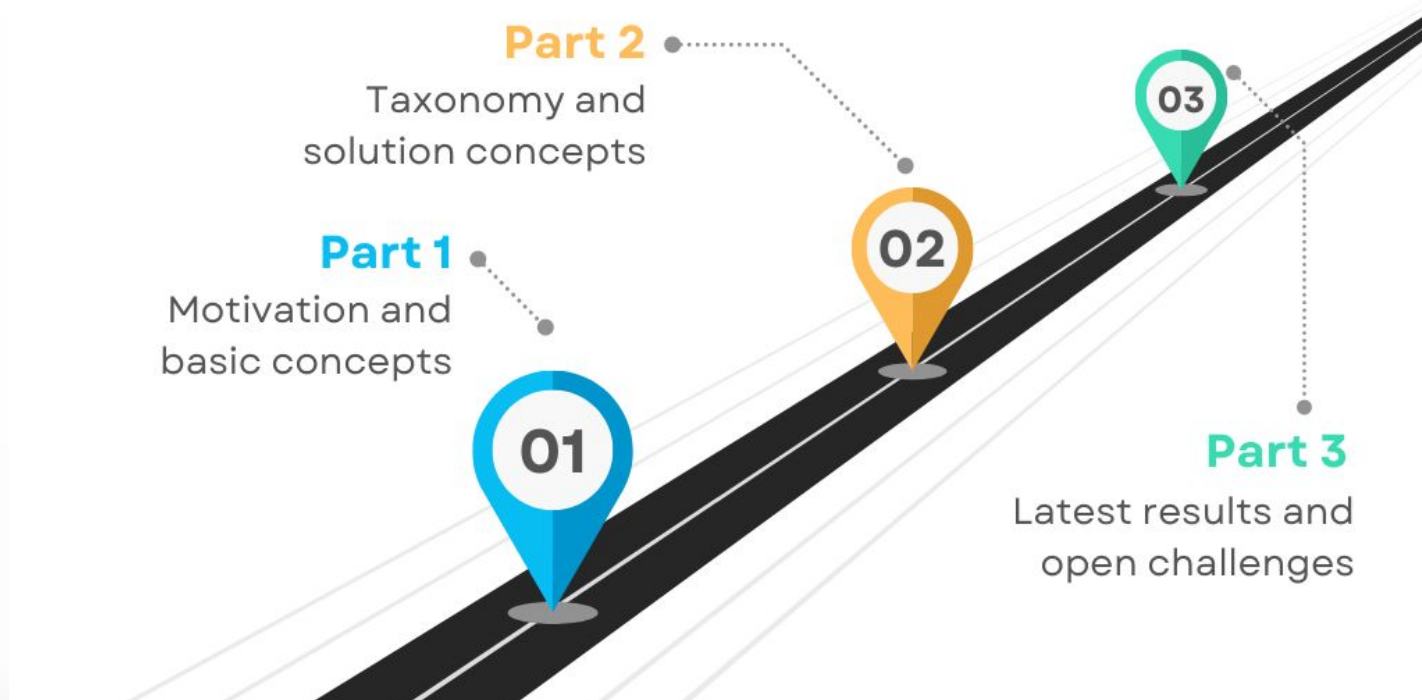
- (FWO) Postdoctoral Fellow at the Artificial Intelligence Research Group, VUB, Belgium
- Project: Decision-making in team-reward multi-objective multi-agent domains



 @rox_teo

<http://roxanaradulescu.com>

Tutorial Roadmap



Part 1 - Multi-objective decision making in multi-agent systems

Motivation and basic concepts



Going to the conference

Two players

- rewards are public
- utility is private

MONFG

Why hard?

	Taxi	Tram	Walking
Taxi	(10€, 5min); (10€, 5min)	(20€, 5min); (2€, 15min)	(20€, 5min); (0€, 35min)
Tram	(2€, 15min); (20€, 5min)	(2€, 15min); (2€, 15min)	(2€, 15min); (0€, 35min)
Walking	(0€, 35min); (20€, 5min)	(0€, 35min); (2€, 15min)	(0€, 35min); (0€, 35min)

Why?

Multiple objectives

Because life is not simple

- What are your objectives for your current research project?
 - Publishing asap?
 - Quality of conference/journal?
 - Collaboration potential?
 - Flag-posting?
 - Increasing funding potential?
 - Finishing your PhD?



Because life really is not simple

- What are your objectives for your current research project?
 - Publishing asap?
 - Quality of conference/journal?
 - Collaboration potential?
 - Flag-posting?
 - Increasing funding potential?
 - Finishing your PhD?
- How about your co-authors?



Multiple objectives!

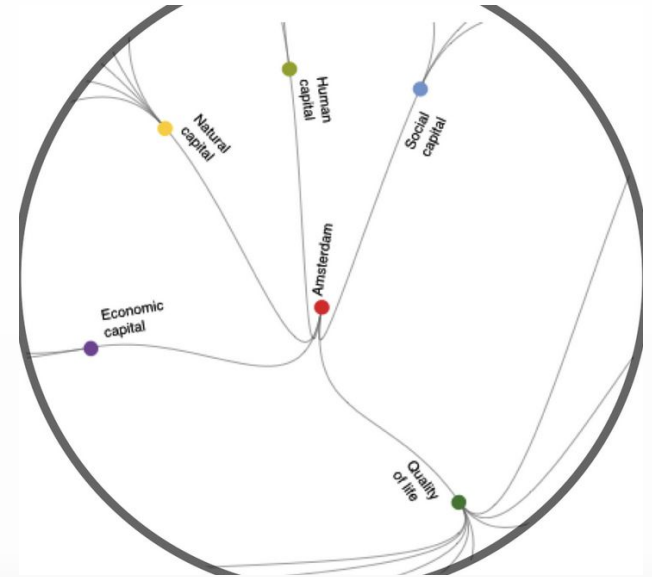
- Most decision problems have multiple objectives
- Cannot scalarise a priori
 - Unknown, uncertain, or private utility
 - Non-linear utility
 - Changeable preferences/utility
 - Adjustability
 - Explainability for oversight and review purposes
- To scalarise is to throw away information

More and more MO

- AI has ever increasing impact on people's lives
- Ethical aspects more important
 - Human-aligned AI is a multi-objective problem [Vamplew et al., 2018]
- Explainability more important
 - Legal frameworks incoming
- Environmental concerns

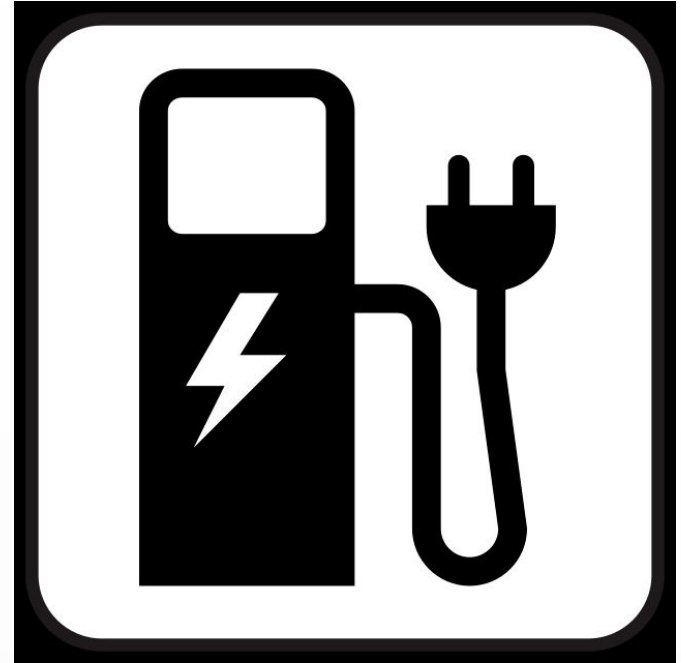
Policy level / paradigm shifts

- New ways of thinking are premutating the policy domain.
- Amsterdam: Brede Welvaart (Broad Wellbeing)
- Both EU and business domain: ESG (environmental, social, governance)



Example: electric vehicle charging

- meeting demands
- minimising costs
- preventing grid overloads



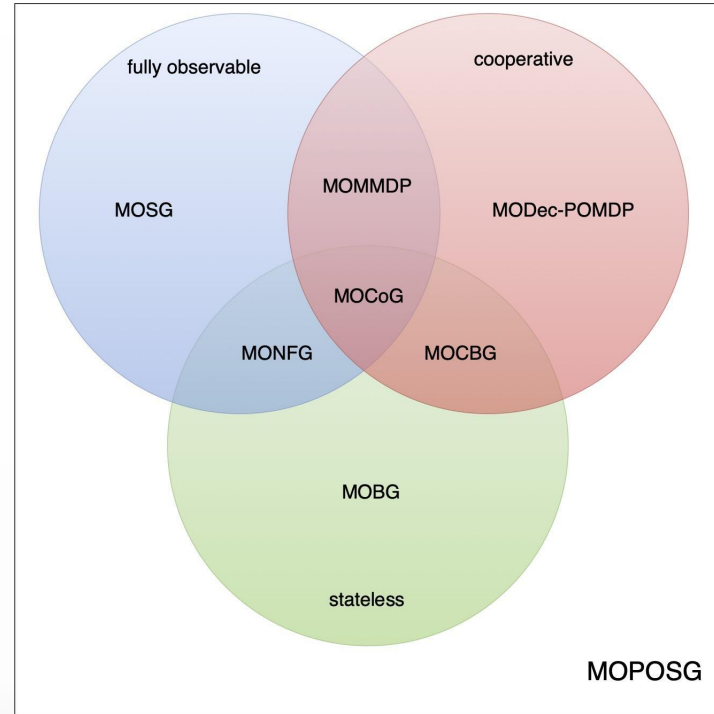
Modelling and dealing w/

Multiple objectives

User utility is central to modelling

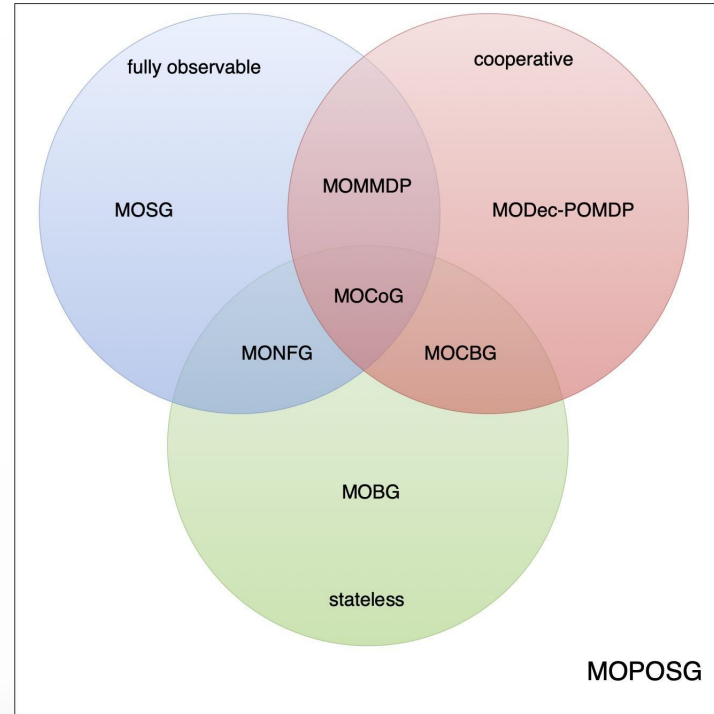
- User utility determines what is desirable for agents
- Stems from meaningful objectives (to the user)
 - Explainable
 - E.g., euros, minutes
- Identifying objectives
 - And then events that trigger rewards
- Decision-theoretic problem setting

MOPOSG



Models:
On the basis of rewards (in objectives) and observations (about states).

MOPOSG



Models:

On the basis of rewards (in objectives) and observations (about states).

But utility is not yet modelled!

Life is still not simple

- What are your objectives for your current research project?
 - Publishing asap?
 - Quality of conference/journal?
 - Collaboration potential?
 - Flag-posting?
 - Increasing funding potential?
 - Finishing your PhD?
- Setting?



Life is still not simple at all?

- What are your objectives for your current research project?
 - Publishing asap?
 - Quality of conference/journal?
 - Collaboration potential?
 - Flag-posting?
 - Increasing funding potential?
 - Finishing your PhD?
- Truly cooperative though?



Policy-based example

- Making a city climate adaptable requires a lot of changes (on almost every street)
 - Green management
 - Water management
 - Circular economy
 - ...
- It also has a lot of impact besides Environmental:
 - Social, disturbing people's live rhythms
 - Economical, ...
- Many stakeholders (citizens, businesses, etc.), many neighbourhoods

Utility-based approach

- Utility function, u_i , maps vector to scalar utility
- Total preference order (can always make a decision between alternatives)
- Utility determines what is optimal within available policies

Utility-based approach

- Solution should be derived from utility
 - Not axiomatically assumed
- This leads to a taxonomy based on rewards and utilities (Part 2)

How to deal with MO problems

- Collect available information about user utility.
- Decide which policies (e.g., stochastic vs deterministic) are allowed.
- Derive the optimal solution concept from the resulting information of the first two points.
- Select or design an algorithm that fits the solution concept.
- When multiple policies are required for the solution, design a method for the user to select the desired policy among these optimal policies.

Short break



Part 2 - Structuring the MOMADM field

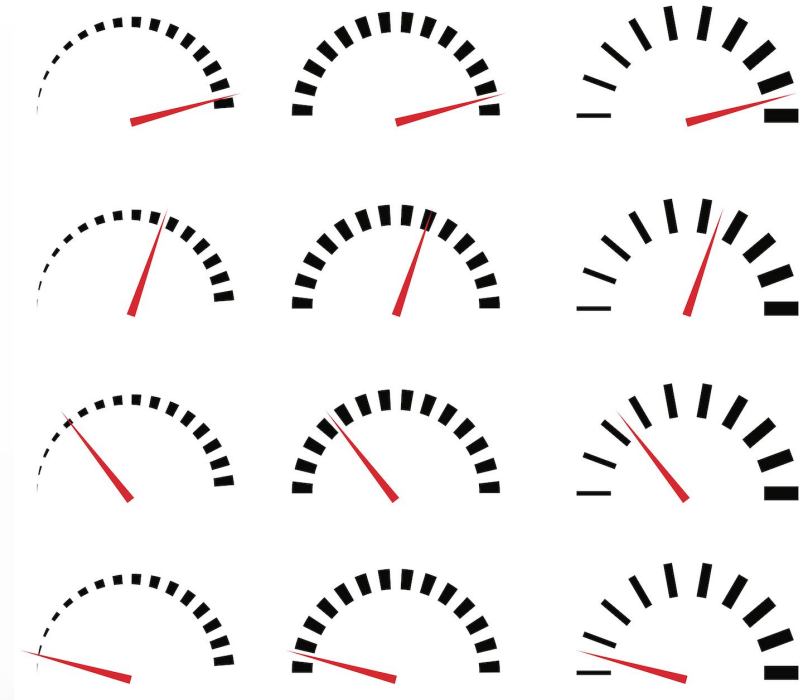
Taxonomy and solution concepts



Optimisation criteria

- Vectorial reward function
- Utility-based perspective

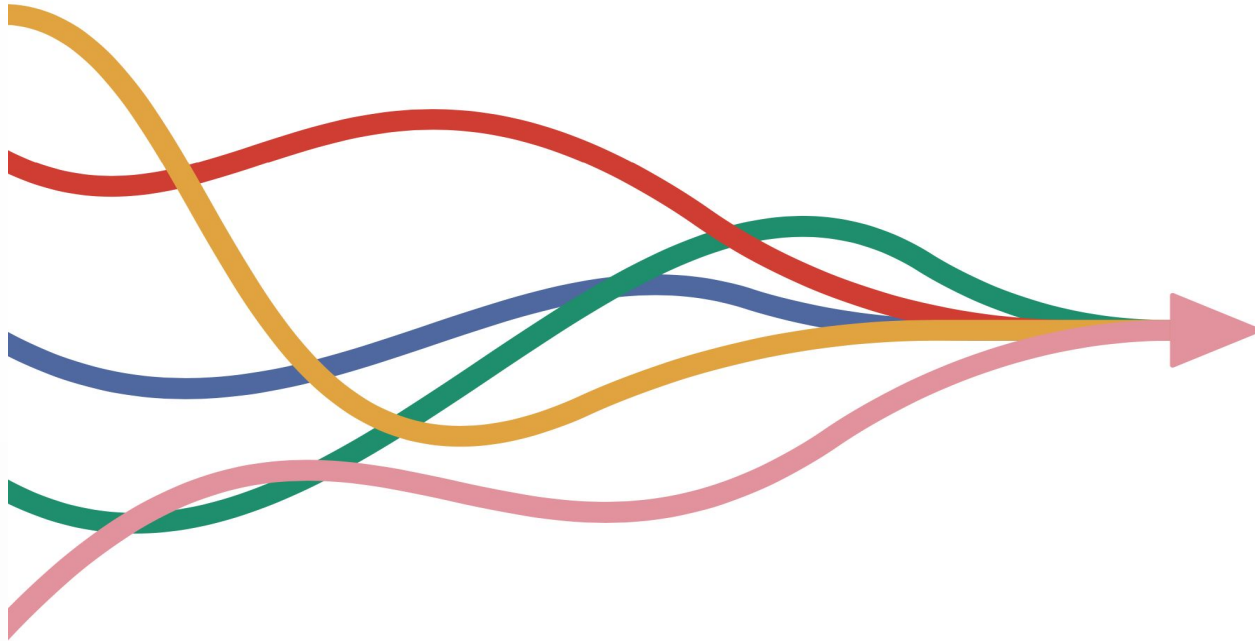
$$u_i: \mathbb{R}^d \rightarrow \mathbb{R}$$



Optimisation criteria



Optimisation criteria



Optimisation criteria



- Expected Scalarised Returns (ESR)
 - Calculate the expectation of the utility from the payoffs
 - Utility of an individual policy execution

Optimisation criteria



- Expected Scalarised Returns (ESR)
 - Calculate the expectation of the utility from the payoffs
 - Utility of an individual policy execution

- Scalarised Expected Returns (SER)
 - Calculate the utility of the expected payoff
 - Utility of the average payoff from several executions of the policy

Optimisation criteria



- Expected Scalarised Returns (ESR)

$$V_u^\pi = \mathbb{E} \left[u \left(\sum_{t=0}^{\infty} \gamma^t \mathbf{r}_t \right) \mid \pi, \mu_0 \right]$$

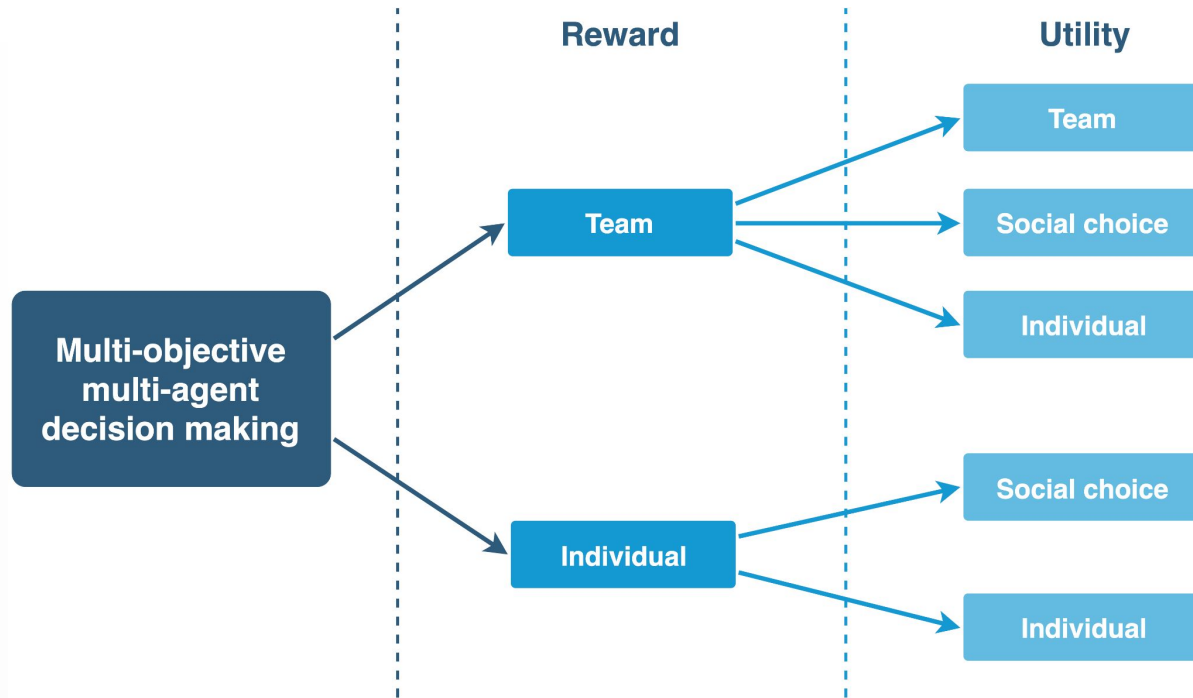


- Scalarised Expected Returns (SER)

$$V_u^\pi = u \left(\mathbb{E} \left[\sum_{t=0}^{\infty} \gamma^t \mathbf{r}_t \mid \pi, \mu_0 \right] \right)$$



Taxonomy



Rădulescu, R., Mannion, P., Roijers, D. M., & Nowé, A. (2020). Multi-objective multi-agent decision making: a utility-based analysis and survey. *Autonomous Agents and Multi-Agent Systems*, 34(1), 1-52.

Taxonomy



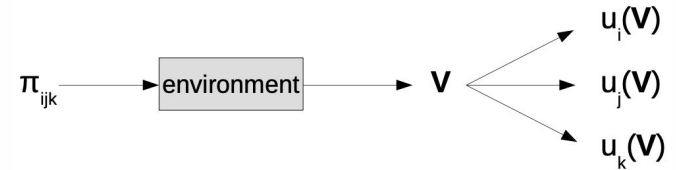
Examples - Team Reward

- Team utility
 - a company that aims to be environmentally responsible, while maximising profits



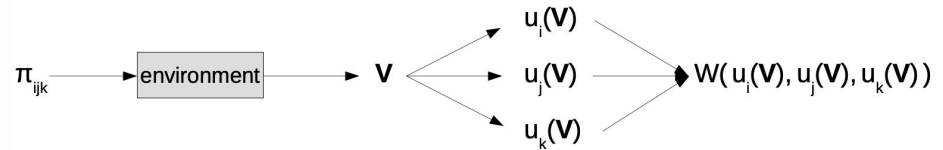
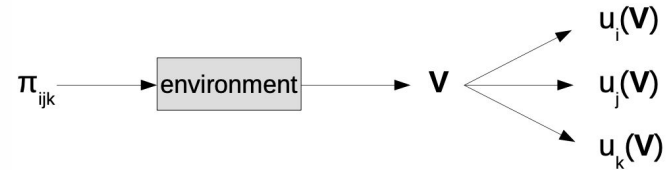
Examples - Team Reward

- Team utility
- Individual utility
 - Climate change policies, resource management



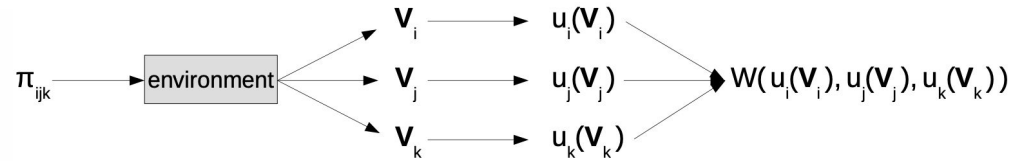
Examples - Team Reward

- Team utility
- Individual utility
- Social Choice
 - urban planning/environmental management/social welfare policies



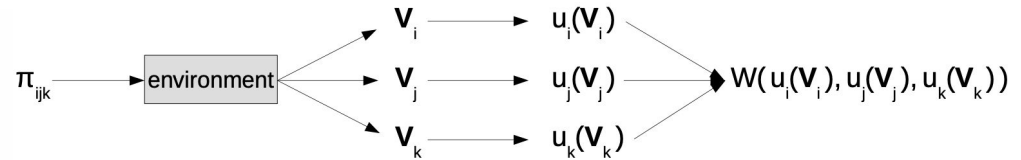
Examples - Individual Reward

- Social choice
 - international trade negotiations

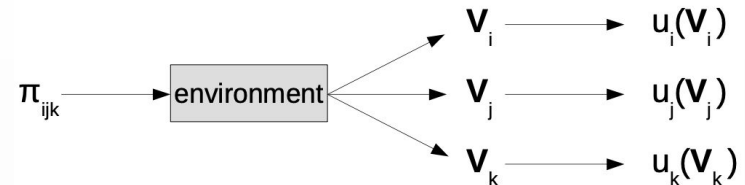


Examples - Individual Reward

- Social choice
 - international trade negotiations



- Individual utility
 - participating in city traffic, work commutes



Solution concepts

		UTILITY		
		TEAM	SOCIAL CHOICE	INDIVIDUAL
REWARD	TEAM	Coverage sets	Mechanism design	Coverage sets (+ Negotiation) Equilibria and stability concepts
	INDIVIDUAL		Mechanism design	Equilibria and stability concepts Coverage Sets as best responses

Coverage sets

- Contain at least one optimal policy for each possible utility function
- **TRTU**: rewards and derived utility is shared between agents, with one utility function selected during execution
- **TRIU**: agent can (contractually) agree which policy to execute
- **IRIU**: set of possible best responses to the behaviour of other agents

		UTILITY		
		TEAM	SOCIAL CHOICE	INDIVIDUAL
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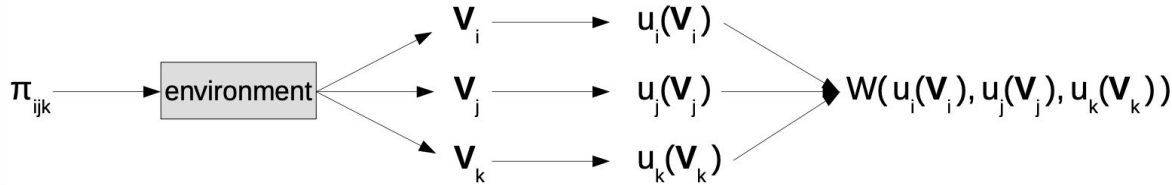
Coverage sets: negotiation

- Automated negotiation
 - Autonomous negotiating agents, representing their user's interests/preferences
 - Reach a compromise that satisfies all the involved parties
 - Pursue equity (i.e., fairness and justice)
- Baarslag, T., Kaisers, M., Gerding, E., Jonker, C. M., & Gratch, J. (2017). When will negotiation agents be able to represent us? The challenges and opportunities for autonomous negotiators. International Joint Conferences on Artificial Intelligence.
- Aydođan, R., & Jonker, C. M. (2023). A Survey of Decision Support Mechanisms for Negotiation. In Recent Advances in Agent-Based Negotiation: Applications and Competition Challenges (pp. 30-51). Singapore: Springer Nature Singapore.

Social Welfare and Mechanism Design

- System perspective: what is a socially desirable outcome

		UTILITY		
		TEAM	SOCIAL CHOICE	INDIVIDUAL
REWARD	TEAM	Coverage sets	Mechanism design	Coverage sets (+ Negotiation) Equilibria and stability concepts
	INDIVIDUAL		Mechanism design	Equilibria and stability concepts Coverage Sets as best responses

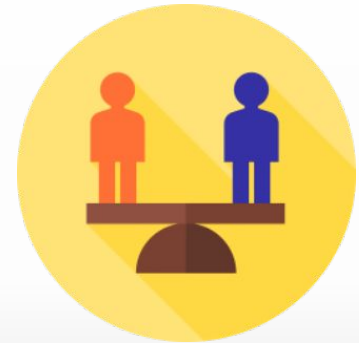


Design a system that forces agents to be truthful about their utilities and leads to optimal solution under W

Equilibria and stability concepts

- Stable outcomes from which self-interested agents have no incentive to deviate
- Nash equilibria, correlated equilibria, cyclic equilibria, coalition formation

		UTILITY		
		TEAM	SOCIAL CHOICE	INDIVIDUAL
REWARD	TEAM	Coverage sets	Mechanism design	Coverage sets (+ Negotiation) Equilibria and stability concepts
	INDIVIDUAL		Mechanism design	Equilibria and stability concepts Coverage Sets as best responses



Nash Equilibrium

- No agent can improve their utility by unilaterally deviating from the joint strategy π^{NE}

- Nash equilibrium under SER:

$$\mathbb{E}u_i [\mathbf{p}_i(\pi_i^{\text{NE}}, \pi_{-i}^{\text{NE}})] \geq \mathbb{E}u_i [\mathbf{p}_i(\pi_i, \pi_{-i}^{\text{NE}})]$$

- Nash equilibrium under ESR:

$$u_i [\mathbb{E}\mathbf{p}_i(\pi_i^{\text{NE}}, \pi_{-i}^{\text{NE}})] \geq u_i [\mathbb{E}\mathbf{p}_i(\pi_i, \pi_{-i}^{\text{NE}})]$$

Correlated Equilibrium - SO

- Introduced by Aumann, in 1974

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- Introduced by Aumann, in 1974
- Correlated strategy - probability vector σ on A
- External mechanism
- No agent can improve their utility by unilaterally deviating from the recommendation of the correlated signal
- A correlated strategy σ^{CE} is a CE if: $\mathbb{E}p_i(\sigma^{CE}) \geq \mathbb{E}p_i(\delta_i(\sigma^{CE}))$

for any strategy modification $\delta_i : A_i \rightarrow A_i$

Correlated Equilibrium - SO

- Correlated equilibria in real-life:



Correlated Equilibrium

- Correlated equilibria under SER:

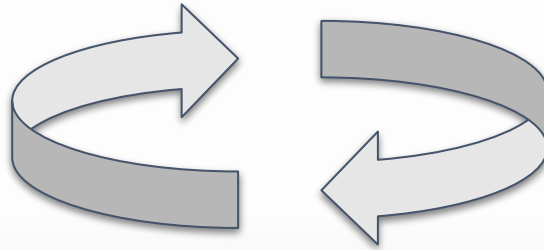
$$u_i \left[\mathbb{E} \mathbf{p}_i(\sigma^{CE}) \right] \geq u_i \left[\mathbb{E} \mathbf{p}_i(\delta_i(\sigma^{CE})) \right]$$

- Correlated equilibria under ESR:

$$\mathbb{E} u_i \left(\mathbf{p}_i(\sigma^{CE}) \right) \geq \mathbb{E} u_i \left(\mathbf{p}_i(\delta_i(\sigma^{CE})) \right)$$

Other solution concepts

- Cyclic Nash equilibria
 - No agent can improve their utility by unilaterally deviating from a joint cyclic strategy



Multi-Objective Normal Form Games

- Introduced by Blackwell in 1956
- MONFG - tuple (N, A, \mathbf{p}) , with $n \geq 2$ and $C \geq 2$ objectives, where:
 - $N = \{1, \dots, n\}$ – set of players
 - $A = A_1 \times \dots \times A_n$ – set of actions
 - $\mathbf{p} = (\mathbf{p}_1, \dots, \mathbf{p}_n)$ – vectorial payoffs

Example - SER

$$u(p_1, p_2) = p_1 \cdot p_2$$

	A	B
A	(10, 2); (10, 2)	(0, 0); (0, 0)
B	(0, 0); (0, 0)	(2, 10); (2, 10)

Example - Nash equilibrium

$$u(p_1, p_2) = p_1 \cdot p_2$$

$$u(10, 2) = 10 \cdot 2 = 20$$

	A	B
A	(10, 2); (10, 2)	(0, 0); (0, 0)
B	(0, 0); (0, 0)	(2, 10); (2, 10)



Example - Cyclic Nash equilibrium

$$u(p_1, p_2) = p_1 \cdot p_2$$

$$u\left(\frac{10+2}{2}, \frac{2+10}{2}\right) = u(6, 6) = 36$$

- Joint cyclic strategy
 - Player 1: {A, B}
 - Player 2: {A, B}

	A	B
A	(10, 2); (10, 2)	(10, 0); (0, 0)
B	(0, 0); (0, 0)	(2, 10); (2, 10)

Example - Correlated equilibrium

$$u(p_1, p_2) = p_1 \cdot p_2$$

$$u\left(\frac{10+2}{2}, \frac{2+10}{2}\right) = u(6, 6) = 36$$

	A	B
A	(10, 2); (10, 2)	(0, 0); (0, 0)
B	(0, 0); (0, 0)	(2, 10); (2, 10)

- Correlated strategy σ
 - 50% (A, A)
 - 50% (B, B)

Part 3 - SOTA

Latest results and open challenges



(Im)balancing Act Game

- 2 players, 2 objective
- Same payoff vector for both players

	L	M	R
L	[4,0]	[3,1]	[2,2]
M	[3,1]	[2,2]	[1,3]
R	[2,2]	[1,3]	[0,4]

$$u_1([p_1, p_2]) = p_1^2 + p_2^2$$
$$u_2([p_1, p_2]) = p_1 \cdot p_2$$

Let's play the (Im)balancing Act Game



https://docs.google.com/forms/d/e/1FAIpQLSfHyr_yLOVsLSyOWDAXvcfecCAM4L2aoqbdSUh19XQocZS9Dg/viewform?vc=0&c=0&w=1&flr=0

ESR Equilibrium

- equilibrium 1: (0.75, 0, 0.25) and (0, 1, 0)
expected utilities: 10 and 3
- equilibrium 2: (0.25, 0, 0.75) and (0, 1, 0)
expected utilities: 10 and 3

ESR	L	M	R
L	16,0	10,3	8,4
M	10,3	8,4	10,3
R	8,4	10,3	16,0

	L	M	R
L	[4,0]	[3,1]	[2,2]
M	[3,1]	[2,2]	[1,3]
R	[2,2]	[1,3]	[0,4]

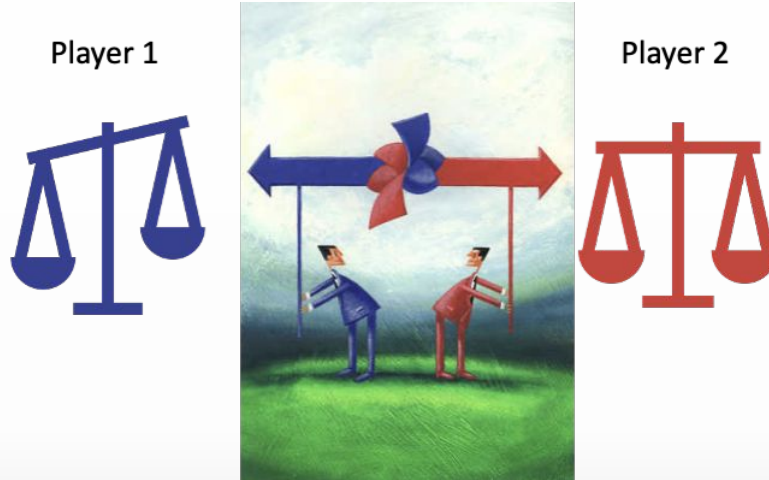
$$u_1([p_1, p_2]) = p_1^2 + p_2^2$$

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Rădulescu, R., Mannion, P., Zhang, Y., Roijers, D. M., & Nowé, A. (2020). A utility-based analysis of equilibria in multi-objective normal-form games. *The Knowledge Engineering Review*, 35.

SER Equilibrium?

- In finite MONFGs, where each agent seeks to maximise the utility under **SER**, **Nash equilibria need not exist.**



	L	M	R
L	[4,0]	[3,1]	[2,2]
M	[3,1]	[2,2]	[1,3]
R	[2,2]	[1,3]	[0,4]

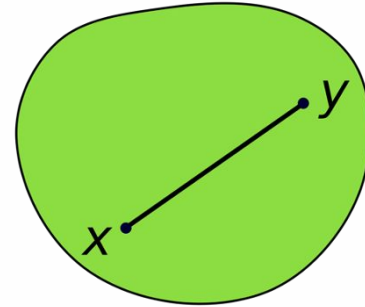
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Bridging continuous games and MONFGs

- Continuous games:
 - Single objective
 - Infinite number of pure strategies
 - Continuous payoff functions
 - Benefit from many theoretical results
 - Algorithmically challenging

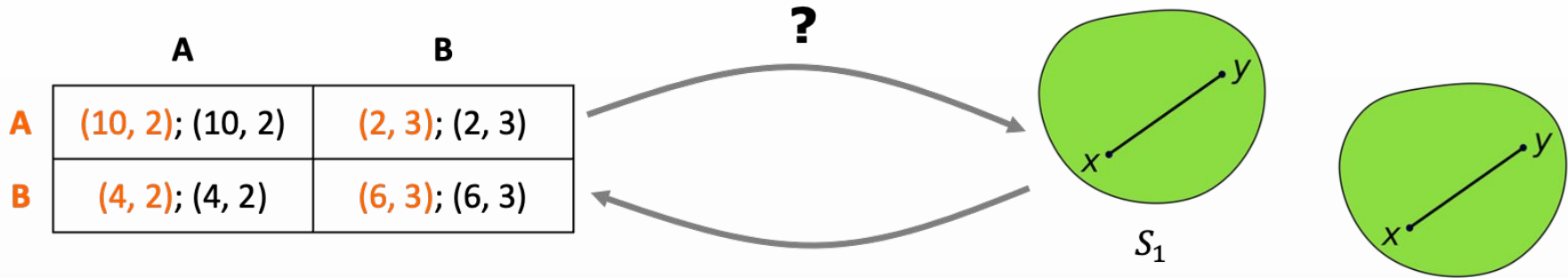


Assumption: convex strategy set

Röpke, W., Groenland, C., Rădulescu, R., Nowé, A., & Roijers, D. M. (2023). Bridging the Gap Between Single and Multi Objective Games. *AAMAS 2023*.

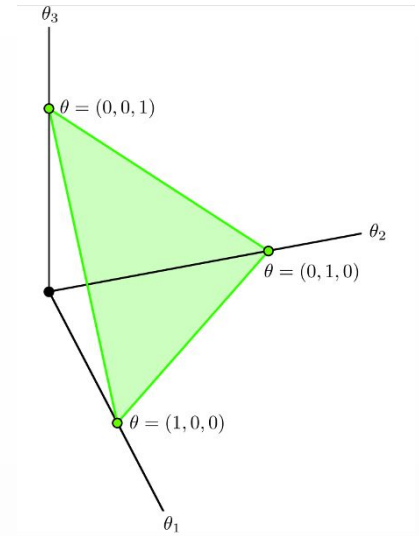
Bridging continuous games and MONFGs

- Build mapping between MONFGs and continuous games
- Ensure that it preserves key dynamics
- Leverage the link for theoretical and algorithmic improvements



Bridging continuous games and MONFGs

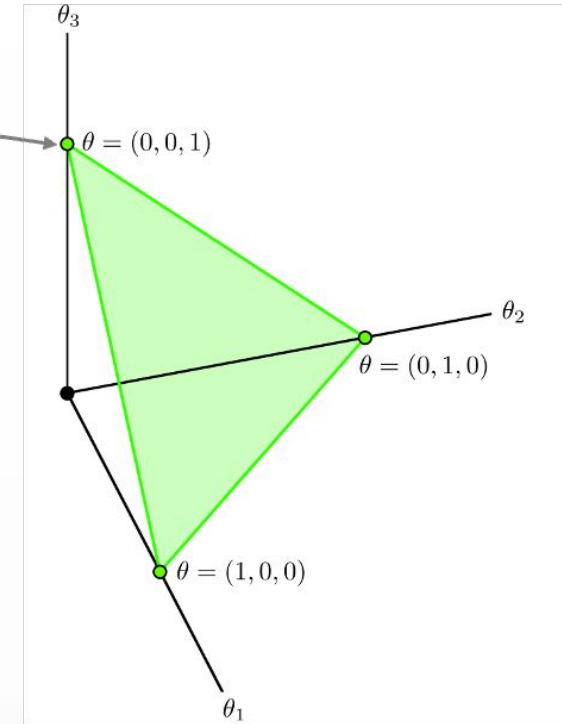
- Every mixed strategy in the MONFG becomes a pure strategy in the continuous game



Röpke, W., Groenland, C., Rădulescu, R., Nowé, A., & Roijers, D. M. (2023). Bridging the Gap Between Single and Multi Objective Games. *AAMAS 2023*.

Bridging continuous games and MONFGs

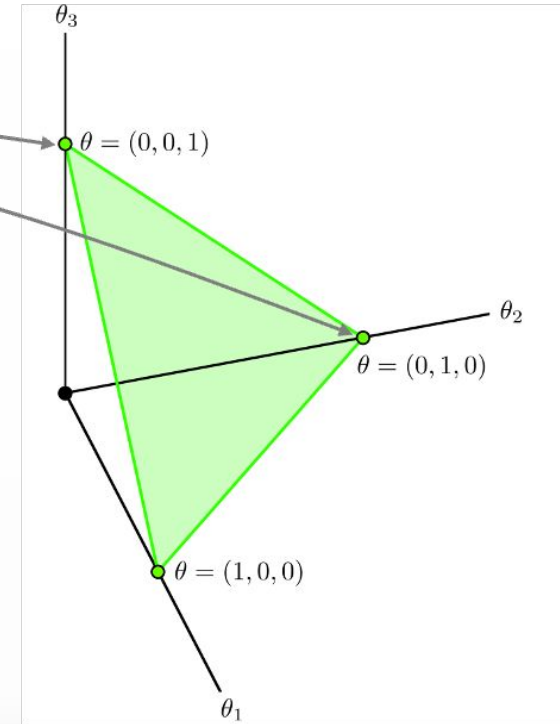
	A	B	C
A	(4, 1); (4, 1)	(1, 2); (4, 2)	(2, 1); (1, 2)
B	(3, 1); (2, 3)	(3, 2); (6, 3)	(1, 2); (2, 1)
C	(1, 2); (2, 1)	(2, 1); (1, 2)	(1, 3); (1, 3)



Bridging continuous games and MONFGs

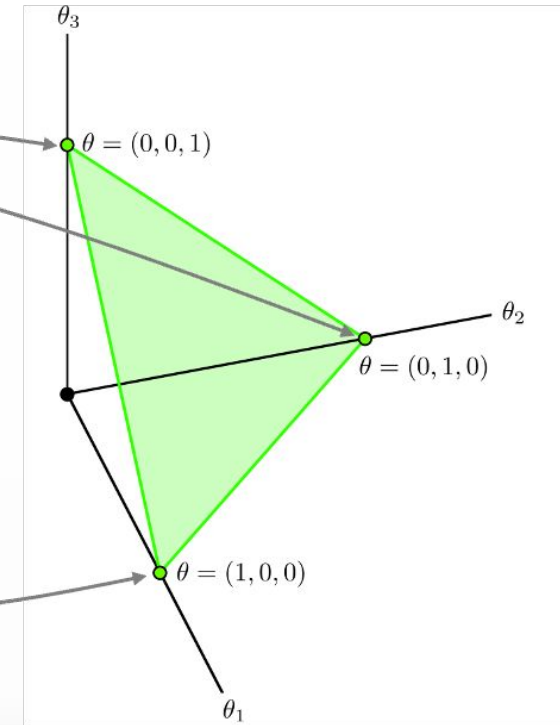
A B C

A	(4, 1); (4, 1)	(1, 2); (4, 2)	(2, 1); (1, 2)
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Bridging continuous games and MONFGs

	A	B	C
A	(4, 1); (4, 1)	(1, 2); (4, 2)	(2, 1); (1, 2)
B	(3, 1); (2, 3)	(3, 2); (6, 3)	(1, 2); (2, 1)
C	(1, 2); (2, 1)	(2, 1); (1, 2)	(1, 3); (1, 3)

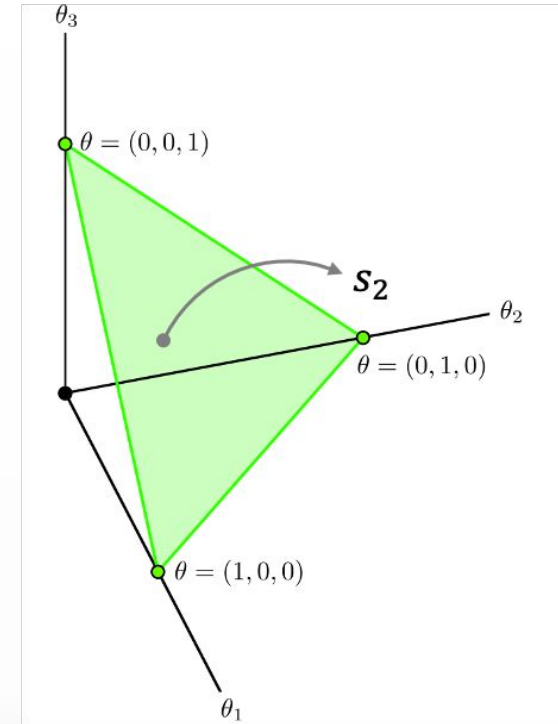


Bridging continuous games and MONFGs

$\frac{1}{4}$ $\frac{1}{4}$ $\frac{2}{4}$

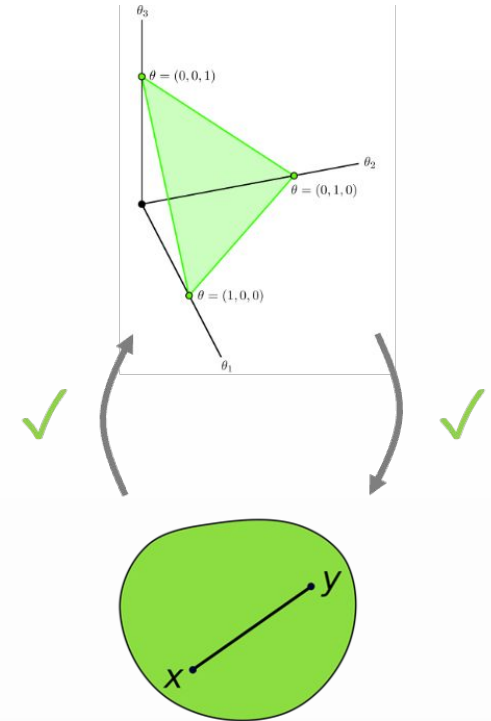
A **B** **C**

A	(4, 1); (4, 1)	(1, 2); (4, 2)	(2, 1); (1, 2)
B	(3, 1); (2, 3)	(3, 2); (6, 3)	(1, 2); (2, 1)
C	(1, 2); (2, 1)	(2, 1); (1, 2)	(1, 3); (1, 3)



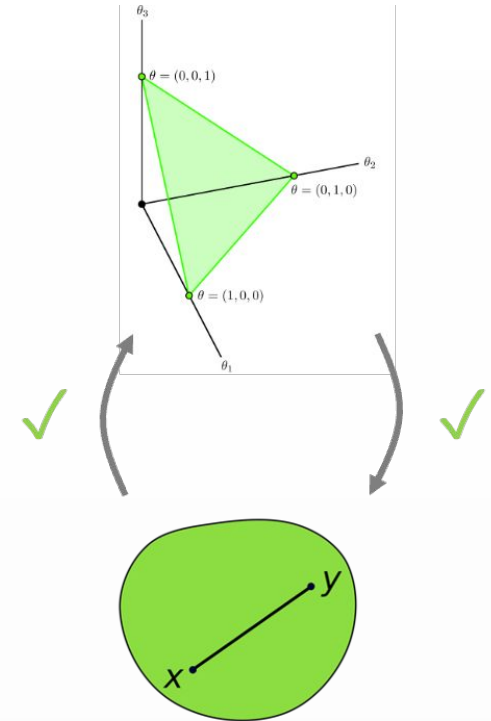
Theoretical insights

- Mixed strategy equilibria in the MONFG are pure strategy equilibria in the continuous game
- Continuous games are not guaranteed to have a pure strategy Nash equilibrium
 - ▶ Nash equilibria are not guaranteed in MONFGs



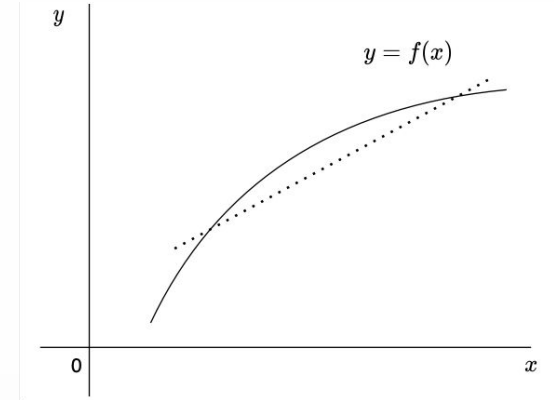
More results

- **Bridging the Gap Between Single and Multi Objective Games:** Röpke, W., Groenland, C., Rădulescu, R., Nowé, A., & Roijers, D. M., AAMAS 2023
- Wednesday (10:45 - 12:30): Equilibria and Complexities of Gamesc session



NE Existence Guarantees

- Existence is guaranteed with (quasi)concave utility functions
 - Used in economics as well
 - Represents “well-behaved” preferences
- Intuition
 - MONFGs can be reduced to continuous games
 - In these game it is known that a pure strategy NE exists when assuming only quasiconcave utility functions
 - This equilibrium is also an equilibrium in the original MONFG



Röpke, W., Roijers, D. M., Nowé, A., & Rădulescu, R. (2022). **On nash equilibria in normal-form games with vectorial payoffs.** *Autonomous Agents and Multi-Agent Systems*, 36(2), 53.

Non-existence

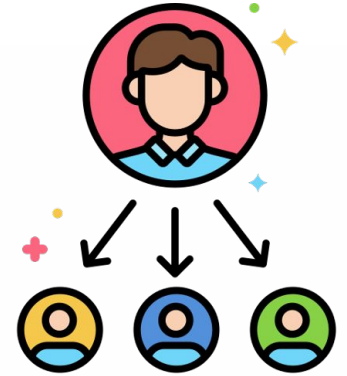
- We can show that no Nash equilibrium exists in this game
 - With **strict convex utility functions**

	A	B
A	(2, 0); (1, 0)	(1, 0); (0, 2)
B	(0, 1); (2, 0)	(0, 2); (0, 1)

$$u_1(p_1, p_2) = u_2(p_1, p_2) = p_1^2 + p_2^2$$

Commitment and Cyclic Strategies

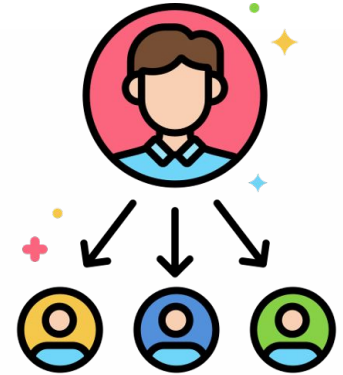
- Commitment
 - One or more players commit to playing a specific strategy
 - Other players condition their own strategies on this commitment
- Leadership equilibria (in two-player games)
 - The leader cannot improve their utility given that the follower plays a best-response
- Weak/strong leadership equilibria
 - Prescribes how an opponent selects their best-response



Röpke, W., Roijers, D. M., Nowé, A., & Rădulescu, R. (2021). **Preference Communication in Multi-Objective Normal-Form Games**. *Neural Computing and Applications (in press)*.

Commitment and Cyclic Strategies

- Commitment can be strictly better than all Nash equilibria
 - Commit may avoid the “fixed-point death trap”



$$u(p_1, p_2) = p_1 \cdot p_2$$

A

B

Nash equilibrium

$$u(10, 2) = 10 \cdot 2 = 20$$

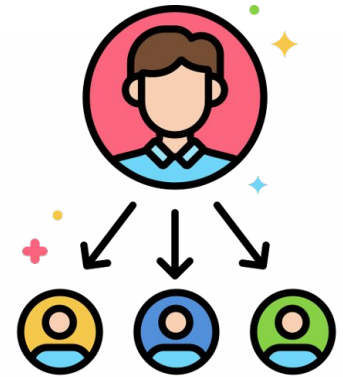
A	(10, 2); (10, 2)	(0, 0); (0, 0)
B	(0, 0); (0, 0)	(2, 10); (2, 10)



Theoretical considerations

- Commitment can be strictly better than all Nash equilibria
 - Commit may avoid the “fixed-point death trap”

The optimal mix is to play
50% (A, A) and 50% (B, B)



$$u\left(\frac{10 + 2}{2}, \frac{2 + 10}{2}\right) = u(6, 6) = 36$$

$$u(p_1, p_2) = p_1 \cdot p_2$$

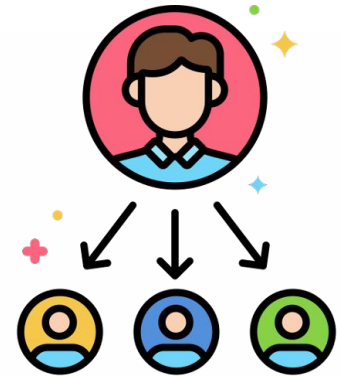
	A	B
A	(10, 2); (10, 2)	(0, 0); (0, 0)
B	(0, 0); (0, 0)	(2, 10); (2, 10)

Blue arrows indicate that the diagonal elements (A,A) and (B,B) are strictly preferred to the off-diagonal elements (A,B) and (B,A).

Theoretical considerations

- Commitment can be strictly better than all Nash equilibria
 - Commit may avoid the “fixed-point death trap”

The optimal mix is to play
50% (A, A) and 50% (B, B)



$$u\left(\frac{10 + 2}{2}, \frac{2 + 10}{2}\right) = u(6, 6) = 36$$

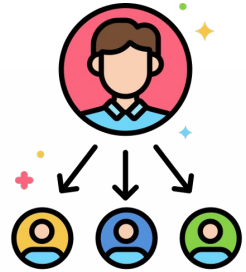
- Joint cyclic strategy
 - Player 1: {A, B}
 - Player 2: {A, B}

$$u(p_1, p_2) = p_1 \cdot p_2$$

	A	B
A	(10, 2); (10, 2)	(0, 0); (0, 0)
B	(0, 0); (0, 0)	(2, 10); (2, 10)

Theoretical considerations

- Commitment is not guaranteed to be as good as a Nash equilibrium
 - If a player commits to a strategy, a malicious player might exploit this
 - This has implications for a range of real-world applications
- Cyclic Nash equilibria may exist when no stationary equilibrium exists
 - Stable solutions can still exist
 - Provides a valid alternative for the goal of a learning algorithm



Open questions

- Commitment and cyclic strategies
 - When can we guarantee that commitment cannot be exploited?
 - What is the link between correlated equilibria and hierarchical equilibria?
 - How to extend the Stackelberg game model to n-player games?
 - Open computational problems
 - Algorithm for learning or computing optimal commitment strategies?
 - How to learn hierarchical strategies?

Relations between optimisation criteria

- **Mixed strategies**

- **No relation** between both optimisation criteria **in general**

$$u(x, y) = 0.1 * x + \max(0, x) * \max(0, y)$$

	A	B
A	(1, 0); (1, 0)	(0, 1); (0, 1)
B	(0, 1); (0, 1)	(-10, 0); (-10, 0)

Multi-objective reward vectors

	A	B
A	0.1; 0.1	0; 0
B	0; 0	-0.1; -0.1

Scalarised utility for both agents

No sharing of number of equilibria or equilibria themselves

Relations between optimisation criteria

- **Pure strategies**
 - Pure strategy equilibrium under SER is also one under ESR
 - Bidirectional when assuming (quasi)convex utility functions
- We can extend this to **blended settings**
 - Pure strategy equilibrium under SER is also one in any blended setting
 - Bidirectional when assuming (quasi)convex utility functions

MOCGs for ESR with Generative Flow Models

- Team reward, team utility
- ESR set: policies require full distributions over returns rather than expected value to evaluate
 - real-valued non-volume preserving transformations
- Distributional Multi-Objective Variable Elimination (DMOVE)



[source](#)

Open questions

- Results for more complex (e.g., sequential, partially observable) settings
- Integrated pipelines for planning -> negotiation -> execution
- Utility modelling
- Strategic disclosure of utility information to the other agents
- Benchmarks

Multi-Objective Decision Making Workshop

- At ECAI 2023
- Kwaków, Poland
- Workshop:
September 30 / October 1
- Deadline: June 30
- Special Issue: NCAA (IF 5.1)



<https://modem2023.vub.ac.be/>

Thank you for listening

- Feel free to ask any questions now
- Or drop us a message at:
 - d.roijers@amsterdam.nl
 - roxana.radulescu@vub.be
- Or follow/add us on Twitter / LinkedIn
- Special thanks to [Willem Röpke](#) (VUB)!

ご清聴
ありがとうございました



This tutorial was based (primarily) on

- Rădulescu, R., Mannion, P., Roijers, D. M., & Nowé, A. (2020). Multi-objective multi-agent decision making: a utility-based analysis and survey. *Autonomous Agents and Multi-Agent Systems*, 34(1), 1-52.
- Rădulescu, R., Mannion, P., Zhang, Y., Roijers, D. M., & Nowé, A. (2020). A utility-based analysis of equilibria in multi-objective normal-form games. *The Knowledge Engineering Review*, 35.
- Rădulescu, R. (2021). *Decision Making in Multi-Objective Multi-Agent Systems: A Utility-Based Perspective*. Brussels: Crazy Copy Center Productions.
- Röpke, W., Roijers, D. M., Nowé, A., & Rădulescu, R. (2022). Preference communication in multi-objective normal-form games. *Neural Computing and Applications*, 1-26.
- Röpke, W., Roijers, D. M., Nowé, A., & Rădulescu, R. (2022). On Nash equilibria in normal-form games with vectorial payoffs. *Autonomous Agents and Multi-Agent Systems*, 36(2), 53.
- Röpke, W., Groenland, C., Rădulescu, R., Nowé, A., & Roijers, D. M. (2023). Bridging the Gap Between Single and Multi Objective Games. *AAMAS 2023*.